

# MA-Mathematics

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## MA 501. History of Mathematics I. 3 Hours.

Development of mathematical principles and ideas from a historical viewpoint, and their cultural, educational and social significance; earliest origins through Newton and Leibnitz.

**Prerequisites:** MA 125 [Min Grade: C] or MA 225 [Min Grade: C]

## MA 502. History of Mathematics II. 3 Hours.

Development of mathematical principles and ideas from a historical viewpoint, and their cultural, educational and social significance; Newton and Leibnitz through early 20th century.

**Prerequisites:** MA 501 [Min Grade: B] or MA 311 [Min Grade: B]

## MA 511. Integrating Mathematical Ideas. 3 Hours.

This course will integrate ideas from algebra, geometry, probability, and statistics. Emphasis will be on using functions as mathematical models, becoming fluent with multiple representations of functions, and choosing the most appropriate representations for solving a specific problem.

Students will be expected to communicate mathematics verbally and in writing through small group, whole group, and individual interactions.

## MA 513. Mathematics for Elementary and Middle School Teachers. 3 Hours.

Problem solving experiences, inductive and deductive reasoning, patterns and functions, some concepts and applications of geometry for elementary and middle school teachers. Topics include linear and quadratic relations and functions and some cubic and exponential functions. Number sense with the rational number system including fractions, decimals and percents will be developed in problem contexts. An emphasis will be on developing algebraic thinking and reasoning.

## MA 514. Mathematics for Elementary and Middle School Teachers. 3 Hours.

Problem solving experiences, inductive reasoning, concepts and applications of geometry and proportional reasoning for elementary and middle school teachers. Topics include analysis of one, two and three dimensional feature of real objects, ratio and proportionality, similarity and congruence, linear, area, and volume measurement, and the development of mathematically convincing arguments. An emphasis will be on developing thinking and reasoning.

**Prerequisites:** MA 313 [Min Grade: C] or MA 513 [Min Grade: C]

## MA 515. Probabilistic & Stat Reasoning. 3 Hours.

Descriptive and inferential statistics, probability, estimation, hypothesis testing. Reasoning with probability and statistics is emphasized.

**Prerequisites:** MA 313 [Min Grade: C] or MA 513 [Min Grade: C]

## MA 516. Numerical Reasoning. 3 Hours.

Develop understanding of number and improve numerical reasoning skills specifically with regard to place value, number relationship that build fluency with basis facts, and computational proficiency; developing a deep understanding of numerous diverse computational algorithms; mathematical models to represent fractions, decimals and percents, equivalencies and operations with fractions, decimals and percents; number theory including order of operations, counting as a big idea, properties of number, primes and composites, perfect, abundant and significant numbers, and figurate numbers; inductive and deductive reasoning with number.

**Prerequisites:** MA 313 [Min Grade: C] or MA 513 [Min Grade: C]

## MA 517. Extending Algebraic Reasoning. 3 Hours.

Extending Algebraic Reasoning. Extending algebraic and functional reasoning to polynomials, rational, exponential, and logarithmic functions; problem-solving involving transfer among representations (equation, graph, table); proof via symbolic reasoning, contradiction, and algorithm; interpretation of key points on graphs (intercepts, slope, extrema); develop facility and efficiency in manipulating symbolic representations with understanding; appropriate use of technology and approximate versus exact solutions; functions as models.

**Prerequisites:** MA 313 [Min Grade: C] or MA 513 [Min Grade: C]

## MA 519. Special Topics for Teachers. 1-4 Hour.

With permission of instructor, may be used as continuation of any of MA 513 through 518. May be repeated for credit when topics vary.

**Prerequisites:** MA 125 [Min Grade: C] or MA 225 [Min Grade: C]

## MA 534. Algebra I: Linear. 3 Hours.

Abstract vector spaces, subspaces, dimension, bases, linear transformation, matrix algebra, matrix representations of linear transformations, determinants.

**Prerequisites:** MA 124 [Min Grade: C] or MA 126 [Min Grade: C] or MA 226 [Min Grade: C]

## MA 535. Algebra II: Modern. 3 Hours.

Rings, including the rings of integers and of polynomials, integral domains, fields and groups. Homomorphism, isomorphism. As time permits, Galois theory, semi-groups, quotient groups, models, or other areas of algebra may be included. Students present proofs from a list of pre-assigned theorems to the class. Logical correctness and proper mathematical proof-writing style are assessed.

**Prerequisites:** MA 434 [Min Grade: C] or MA 534 [Min Grade: C]

## MA 540. Advanced Calculus I. 3 Hours.

This class covers sequences and series of real numbers, supremum and infimum limits for subsets of the real numbers, the theorem of Bolzano-Weierstrass, Cauchy sequences, continuous functions, intermediate value theorem, uniform continuity, monotone functions. In addition, derivatives - mean value theorem, Taylor's theorem for real functions on a real interval, Riemann integration for functions on a real interval, improper integrals.

## MA 541. Advanced Calculus II. 3 Hours.

This class covers sequences of functions, including pointwise and uniform convergence and the specifics of interchanging limits. Series of functions, including the M-test, differentiation/integration and real analytic functions will be studied. We introduce metric spaces and develop the notions of open and closed sets, completeness and compactness, Cauchy sequences, continuous functions between metric spaces, uniform continuity, Heine-Borel and related theorems, contraction mapping theorem, Arzela-Ascoli theorem.

**Prerequisites:** MA 540 [Min Grade: C]

## MA 544. Vector Analysis. 3 Hours.

Review and applications of multiple integrals, Jacobians and change of variables in multiple integrals; line and surface integrals; theorems of Green, Gauss, and Stokes with application to the physical sciences; computation in spherical and cylindrical coordinates.

**Prerequisites:** MA 227 [Min Grade: C]

## MA 545. Complex Analysis. 3 Hours.

Analytic functions, complex integration and Cauchy's theorem, Taylor and Laurent series, calculus of residues and applications, conformal mappings.

**Prerequisites:** MA 227 [Min Grade: C]

**MA 553. Fourier Analysis. 3 Hours.**

Fourier series, including odd/even functions expansions, complex power series, generalized Fourier series. Convergence, applications to partial differential equations. Fourier transform: basic properties, inversion of the FT, windowing, relation to the Laplace transform. Applications to partial differential equations. Wavelets and signal processing basic functions, transforming wavelets, short time Fourier transform.

**Prerequisites:** MA 252 [Min Grade: C]

**MA 554. Intermediate Differential Equations. 3 Hours.**

Topics from among Frobenius series solutions, Sturm-Liouville systems, nonlinear equations, and stability theory.

**Prerequisites:** MA 252 [Min Grade: C]

**MA 555. Partial Differential Equations I. 3 Hours.**

Classification of second order partial differential equations; background on eigenfunction expansions and Fourier series; integrals and transforms; solution of the wave equation, reflection of waves; solution of the heat equation in bounded and unbounded media; Laplace s equations, Dirichlet and Neumann problems.

**Prerequisites:** MA 252 [Min Grade: C]

**MA 556. Partial Differential Equations II. 3 Hours.**

Classification of second order partial differential equations; background on eigenfunction expansions and Fourier series; integrals and transforms; solutions of the wave equations, reflection of waves; solution of heat equation in bounded and unbounded media; Laplace s equations, Dirichlet and Neumann problems.

**Prerequisites:** MA 252 [Min Grade: C]

**MA 560. Scientific Programming. 3 Hours.**

Programming and mathematical problem solving using Matlab, Python, FORTRAN or C++. Emphasizes the systematic development of algorithms and numerical methods. Topics include computers, floating point arithmetic, iteration, functions, arrays, Matlab graphics, image processing, robotics, GNU/Linux operating system, solving linear systems and differential equation arising from practical situations, use of debuggers and other debugging techniques, and profiling; use of callable subroutine packages like LAPACK and differential equation routines; parallel programming. Assignments and projects are designed to give students a computational sense through complexity, dimension, inexact arithmetic, randomness, simulation and the role of approximation.

**Prerequisites:** MA 126 [Min Grade: C] or MA 226 [Min Grade: C]

**MA 561. Modeling with Partial Differential Equations. 3 Hours.**

Practical examples of partial differential equations; derivation of partial differential equations from physical laws; introduction to MATLAB and its PDE Tool-box, and COMSOL using practical examples; an overview of finite difference and finite element solution methods; specialized modeling projects in topics such as groundwater modeling, scattering of waves, medical and industrial imaging, continuum mechanics and deformation of solids, Fluid mechanics including the class boat race, financial derivative modeling, and acoustic and electromagnetic wave applications. Written project reports required for all homework assignments. Quantitative Literacy and Writing are significant components of this course.

**Prerequisites:** MA 252 [Min Grade: C]

**MA 562. Intro to Stochastic Differential Equations. 3 Hours.**

Stochastic differential equations arise when random effects are introduced into the modeling of physical systems. Topics include Brownian motion and Wiener processes, stochastic integrals and the Ito calculus, stochastic differential equations, and applications to financial modeling, including option pricing.

**Prerequisites:** MA 485 [Min Grade: C] or MA 585 [Min Grade: C]

**MA 566. Introduction to Optimization. 3 Hours.**

Optimization is important in many decision making problems in various areas like engineering, economics and machine learning. Optimization theory deals with finding the best solution(s) or variables of a given objective function. Recently, the area of optimization has received much attention due to the development of highly efficient computational methods for data analysis. The scope of this course covers linear algebra, unconstrained optimization, linear programming, and nonlinear constrained optimization. The topics include linear algebra, linear program, duality, network flows, simplex method, non-simplex method, gradient and conjugate methods, neural network, genetic algorithm and convex optimization. The course will also introduce optimization algorithms and codes via python and matlab.

**Prerequisites:** MA 126 [Min Grade: C] or MA 226 [Min Grade: C]

**MA 567. Gas Dynamics. 3 Hours.**

Euler s equations for inviscid flows, rotation and vorticity, Navier-Stok.

**Prerequisites:** MA 252 [Min Grade: C] and (MA 360 [Min Grade: C] or MA 560 [Min Grade: C])

**MA 568. Numerical Analysis I. 3 Hours.**

Programming for numerical calculations, round-off error, approximation and interpolation, numerical quadrature, and solution of ordinary differential equations. Practice on the computer.

**Prerequisites:** MA 252 [Min Grade: C] and MA 227 [Min Grade: C]

**MA 569. Numerical Analysis II. 3 Hours.**

Iterative solution of systems of nonlinear equations, evaluation of eigenvalues and eigenvectors of matrices, applications to simple partial differential equations, special topics in numerical linear algebra. Practice on the computer.

**Prerequisites:** MA 568 [Min Grade: C]

**MA 570. Differential Geometry. 3 Hours.**

Theory of curves and surfaces: Frenet formulas for curves, first and second fundamental forms of surfaces. Global theory; abstract surfaces, manifolds, Riemannian geometry.

**Prerequisites:** MA 126 [Min Grade: C] or MA 226 [Min Grade: C]

**MA 572. Geometry I. 3 Hours.**

The axiomatic method; Euclidean geometry including Euclidean constructions, basic analytic geometry, transformational geometry, and Klein's Erlangen Program. Students present proofs from a list of pre-assigned theorems to the class. Logical correctness and proper mathematical proof-writing style are assessed.

**Prerequisites:** MA 125 [Min Grade: C] or MA 225 [Min Grade: C]

**MA 573. Geometry II. 3 Hours.**

Analytical geometry, Birkhoff s axioms, and the complex plane; structure and representation of Euclidean isometries; plane symmetries; non-Euclidean (hyperbolic) geometry and non-Euclidean transformations; fractal geometry; algorithmic geometry. Course integrates intuition/ exploration and proof/explanation. Project and report or oral presentation required.

**Prerequisites:** MA 472 [Min Grade: C] or MA 572 [Min Grade: C]

**MA 574. Intro to Topology I. 3 Hours.**

Separable metric spaces, basis and sub-basis, continuity, compactness, completeness, Baire category theorem, countable products, general topological spaces, Tychonov theorem.

**Prerequisites:** MA 126 [Min Grade: C] or MA 226 [Min Grade: C]

**MA 575. Intro to Topology II. 3 Hours.**

Separable metric spaces, basis and sub-basis, continuity, compactness, completeness, Baire category theorem, countable products, general topological spaces, Tychonov theorem.

**Prerequisites:** MA 574 [Min Grade: C]

**MA 584. Mathematical Finance. 3 Hours.**

The notion of no arbitrage. Interest, compounding, bonds. Review of mean, variance, and covariance. Portfolio management: risk and return. Forwards and Futures. Put-call parity. Martingales and conditional expectation. The binomial model. Fundamental theorems of asset pricing. Brownian motion (heuristics). Ito's formula and Girsanov's theorem (heuristics). The Black-Scholes-Merton formula. Interest rates. The binomial model for stochastic interest rates.

**Prerequisites:** (MA 260 [Min Grade: C] or MA 434 [Min Grade: C] or MA 435 [Min Grade: C]) and (MA 485 [Min Grade: C] or MA 585 [Min Grade: C])

**MA 585. Intro to Probability. 3 Hours.**

Probability spaces, combinatorics, conditional probabilities and independence, Bayes rule, discrete and continuous distributions, mean value and variance, moment generation function, joint distributions, correlation, Central Limit Theorem, Law of Large Numbers, random walks, Poisson process.

**Prerequisites:** MA 227 [Min Grade: C] and MA 260 [Min Grade: C]

**MA 586. Mathematical Statistics. 3 Hours.**

Confidence intervals, hypothesis testing, analysis of variance and covariance, maximum likelihood estimates, linear regression, tests of fit, robust estimates and tests.

**Prerequisites:** MA 485 [Min Grade: C] or MA 585 [Min Grade: C]

**MA 587. Advanced Probability. 3 Hours.**

Foundation of probability, conditional probabilities, and independence, Bayes theorem, discrete and continuous distributions, joint distributions, conditional and marginal distributions, convolution, moments and moment generation function, multivariable normal distribution and sums of normal random variables, Markov chains.

**Prerequisites:** MA 485 [Min Grade: B] or MA 585 [Min Grade: B]

**MA 588. Advanced Statistics. 3 Hours.**

Parameter estimations, maximum likelihood estimation, sufficient statistic, hypothesis testing, Neyman-Pearson Lemma, p-value, Kolmogorov-Smirnov test, Anderson-Darling test, P-P plot, Q-Q plot, testing for distribution type, location and scale parameters, mean squared error.

**Prerequisites:** MA 485 [Min Grade: B] or MA 585 [Min Grade: B] or MA 587 [Min Grade: B] or MA 687 [Min Grade: B]

**MA 589. STATISTICAL TECHNIQUES FOR MACHINE LEARNING AND BIG DATA. 3 Hours.**

Topics of statistical learning and how to implement these methods by using R/Python. The course will cover major statistical learning methods and concepts for both supervised and unsupervised learning, such as sampling algorithms; nonparametric tests; model assessment and selection; classification, clustering; and big data analysis.

**Prerequisites:** MA 486 [Min Grade: B] or MA 586 [Min Grade: B]

**MA 590. Mathematics Seminar. 1-3 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 591. Mathematics Seminar. 1-3 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 592. Special Topics in Mathematics. 1-3 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 593. Special Topics in Mathematics. 1-3 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 594. Special Topics in Mathematics. 1-6 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 595. Special Topics in Mathematics. 1-6 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 596. Special Topics in Mathematics. 1-12 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 597. Special Topics in Mathematics. 1-12 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 598. Research in Mathematics. 1-12 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 599. Research in Mathematics. 1-12 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 610. Intro to Set Theory. 3 Hours.**

Set theory, products, relations, orders and functions, cardinal and ordinal numbers, transfinite induction, axiom of choice, equivalent statements.

**MA 631. Linear Algebra. 3 Hours.**

Vector spaces and their bases; linear transformations; eigenvalues and eigenvectors: Jordan canonical form; multilinear algebra and determinants; norms and inner products.

**MA 632. Abstract Algebra. 3 Hours.**

Propositional and predicate logic; set, relations, and functions; the induction principle; Groups, in particular symmetry groups, permutations groups, and cyclic groups; cosets and quotient groups; group homomorphisms; rings, integral domains, and fields; ideals and rings homomorphisms; factorization; polynomial rings.

**Prerequisites:** MA 534 [Min Grade: B] or MA 631 [Min Grade: B]

**MA 637. Graph Theory and Combinatorics. 3 Hours.**

Topics covered include specialized terminology and notation; eulerian and hamiltonian graphs; matrices of graphs and information about graphs obtained from matrices; topological graph theory, including planarity theorems of Kuratowski, Whitney and MacLane and also embeddings of graphs in surfaces of higher genus and in nonorientable surfaces; Menger's theorem and network flows; the graph reconstruction problem; counting techniques, including the Pigeonhole Principle and the use of generating functions; Dilworth's theorem; Sperner's lemma; finite and infinite Ramsey theory; matching theory and the classical theorem of Philip Hall; and, if time permits, the Polya/Redfield theory of enumerations.

**MA 640. MATHEMATICAL ANALYSIS I. 3 Hours.**

The course introduces basic objects in analysis, such as the structure of the real numbers, the rationals, sequences of real numbers, the concepts of  $\lim$ ,  $\liminf$ ;  $\limsup$ . Further on, the Bolzano-Weierstrass theorem and the Cauchy sequences are discussed in detail. The relevant material is in Sections 2.1, 2.2, 2.3, 2.4, [1]. Next, another basic object, continuous functions is introduced and analyzed. In particular, the min-max theorem, the intermediate value theorem, uniform continuity for continuous functions and its relation with continuity, Sections 3.2, 3.3, 3.4, 3.5, 3.6 [1]. Another classical object, the derivative of a function of one variable is introduced. Classical results such as the mean value theorem, the Taylor's theorem for real functions on a real interval are covered along with applications, Sections 4.1, 4.2, 4.3 [1]. Finally, the theory of the Riemann integration for functions on a real interval is build. The relevant material is contained in Sections 5.1, 5.2, 5.3, 5.5, [1].

**MA 641. MATHEMATICAL ANALYSIS II. 3 Hours.**

The course is a continuation of MA 640 and provides a necessary prerequisite to a number of standard higher Ph.D. level courses, such as Topology, Measure theory, Numerical Analysis, Functional Analysis etc. Specifically, sequences of functions are introduced, and of particular interest will be pointwise and uniform convergence, interchange of limits to name a few. This is mostly a prerequisite toward an important object in the theory, namely series of functions. Various convergence tests are discussed and analyzed: comparison test, M - test, Dirichlet test, integral test. Finally, the theory of differentiation and integration for series is developed, including properties of power series/real analytic functions. The course finishes with a short introduction to some basic topological objects. Specifically, metric spaces are introduced. Important concepts in this context include open and closed sets, completeness and compactness, Cauchy sequences. Continuous functions between metric spaces and uniform continuity of such functions are discussed, together with various applications. Finally, the Heine-Borel and related theorems, the contraction mapping theorem, and the Arzela-Ascoli theorem are proved in detail, together with relevant applications.

**Prerequisites:** MA 640 [Min Grade: B]

**MA 642. Calculus of Several Variables. 3 Hours.**

Functions of several variables; total and partial derivatives; the Implicit Function Theorem; integration of differential forms; Stokes's Theorem.

**Prerequisites:** MA 541 [Min Grade: B]

**MA 645. Real Analysis I. 3 Hours.**

Abstract measures and integration; positive Borel measures;  $L_p$ -spaces.

**Prerequisites:** MA 642 [Min Grade: B] and MA 670 [Min Grade: B]

**MA 646. Real Analysis II. 3 Hours.**

Complex measures and the Radon-Nikodym theorem; differentiation; integration on product spaces and Fubini's theorem.

**Prerequisites:** MA 645 [Min Grade: B]

**MA 648. Complex Analysis. 3 Hours.**

The algebraic and topological structure of the complex plane; analytic functions; Cauchy's integral theorem and integral formula; power series; elementary functions; and their Riemann surfaces; isolated singularities and residues; the Laurent expansion; the Riemann mapping theorem.

**Prerequisites:** MA 642 [Min Grade: B]

**MA 650. Differential Equations. 3 Hours.**

Separable, linear, and exact first order equations; existence and uniqueness theorems; continuous dependence of solutions on data and initial conditions; first order systems and higher order equations; stability for two-dimensional linear systems; higher order linear systems; boundary value problems; stability theory.

**Prerequisites:** MA 642 [Min Grade: B]

**MA 655. Partial Differential Equations. 3 Hours.**

This course covers first order partial differential equations, elliptic equations, parabolic equations, and hyperbolic equations.

**Prerequisites:** MA 642 [Min Grade: C] or MA 650 [Min Grade: C]

**MA 660. Numerical Linear Algebra. 3 Hours.**

Vector and matrix norms; the singular value decomposition; stability, condition numbers, and error analysis; QR factorization; least squares problems; computation of eigenvalues and eigenvectors; iterative methods.

**Prerequisites:** MA 631 [Min Grade: B]

**MA 661. Modeling With PDE. 3 Hours.**

Practical examples of partial differential equations; derivation of partial differential equations from physical laws; introduction to MATLAB and its PDE Toolbox, and other PDE packages such as FEMLAB using practical examples; brief discussion of finite difference and finite element solution methods; introduction to continuum mechanics and classical electrodynamics; parallel programming using MPI and the mathematics department Beowulf system; specialized modeling projects in topics such as groundwater modeling, scattering of waves, medical and industrial imaging, fluid mechanics, and acoustic and electromagnetic applications.

**MA 665. Partial Differential Equations: Finite Difference Methods. 3 Hours.**

Review of difference methods for ordinary differential equations including Runge-Kutta, multi-step, adaptive step-sizing, and stiffness; finite difference versus finite element; elliptic boundary value problems; iterative solution methods, self-adjoint elliptic problems; parabolic equations including consistency, stability, and convergence, Crank-Nicolson method, method of lines; first order hyperbolic systems and characteristics Lax-Wendroff schemes, methods of lines for hyperbolic equations.

**Prerequisites:** MA 360 [Min Grade: C] or MA 560 [Min Grade: C] or MA 455 [Min Grade: C] or MA 555 [Min Grade: C]

**MA 668. Numerical Analysis I. 3 Hours.**

Integrals, interpolation, rational approximation, numerical solution of ordinary differential equations, iterative solution of algebraic equations in single variable, least squares. Gaussian elimination for solution of linear equations.

**Prerequisites:** MA 670 [Min Grade: B]

**MA 669. Numerical Analysis II. 3 Hours.**

Integrals, interpolation, rational approximation, numerical solution of ordinary differential equations, iterative solution of algebraic equations in single variable, least squares. Gaussian elimination for solution of linear equations.

**Prerequisites:** MA 668 [Min Grade: B]

**MA 670. Topology I. 3 Hours.**

Definition of topologies; closure; continuity; finite product topology; metric spaces; connectedness; completeness and compactness (in particular, in metric spaces).

**Prerequisites:** MA 631 [Min Grade: B] or MA 540 [Min Grade: B] or MA 440 [Min Grade: B]

**MA 671. Topology II. 3 Hours.**

Product topology; quotient spaces; countability and separation axioms; Tychonoff's theorem; homotopy; manifolds; partitions of unity.

**Prerequisites:** MA 670 [Min Grade: B]

**MA 675. Differential Geometry. 3 Hours.**

Local and global theory of curves and surfaces; Fenchel's theorem; the first and second fundamental forms; surface area; Bernstein's theorem; Gauss theorem egregium; local intrinsic geometry of surfaces; Riemannian surfaces; Lie derivatives; covariant differentiation; geodesics; the Riemann curvature tensor; the second variation of arc length; selected topics in the global theory of surfaces.

**Prerequisites:** MA 642 [Min Grade: C]

**MA 687. Advanced Probability. 3 Hours.**

Foundation of probability, conditional probabilities, and independence, Bayes theorem, discrete and continuous distributions, joint distributions, conditional and marginal distributions, convolution, moments and moment generation function, multivariable normal distribution and sums of normal random variables, Markov chains.

**Prerequisites:** MA 485 [Min Grade: B] or MA 585 [Min Grade: B]

**MA 688. Advanced Statistics. 3 Hours.**

Parameter estimations, maximum likelihood estimation, sufficient statistic, hypothesis testing, Neyman-Pearson Lemma, p-value, Kolmogorov-Smirnov test, Anderson-Darling test, P-P plot, Q-Q plot, testing for distribution type, location and scale parameters, mean squared error.

**Prerequisites:** MA 585 [Min Grade: B] or MA 587 [Min Grade: B] or MA 687 [Min Grade: B]

**MA 690. Mathematics Seminar. 1-3 Hour.**

This course covers special topics in mathematics and the applications of the mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 691. Mathematics Seminar. 1-3 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 692. Special Topics in Mathematics. 1-3 Hour.**

This course covers special topics in mathematics and the applications of the mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 693. Special Topics in Mathematics. 1-3 Hour.**

This course covers special topics in mathematics and the applications of the mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 694. Special Topics in Mathematics. 1-6 Hour.**

This course covers special topics in mathematics and the applications of the mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 695. Special Topics in Mathematics. 1-6 Hour.**

This course covers special topics in mathematics and the applications of the mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 696. Special Topics in Mathematics. 1-12 Hour.**

This course covers special topics in mathematics and the applications of the mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 697. Special Topics in Mathematics. 1-12 Hour.**

This course covers special topics in mathematics and the applications of the mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 698. M Lev Non-Thesis Res. 1-12 Hour.**

This course covers special topics in mathematics and the applications of the mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 699. Research for Thesis. 1-12 Hour.**

This course covers special topics in mathematics and the applications of the mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**Prerequisites:** GAC M

**MA 740. Advanced Complex Analysis. 3 Hours.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites: Having passed the Qualifying Exam or permission of instructor.

**MA 745. Functional Analysis I. 3 Hours.**

Normed and Banach spaces; inner product and Hilbert spaces; linear functionals and dual spaces; operators in Hilbert spaces; theory of unbounded sesquilinear forms; Hahn-Banach, open mapping and closed graph theorems; spectral theory.

**Prerequisites:** MA 646 [Min Grade: B]

**MA 746. Functional Analysis II. 3 Hours.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 747. Linear Operators in Hilbert Space. 3 Hours.**

Hilbert space; Bessel's inequality; Parseval's formula; bounded and unbounded linear operators; representation theorems; the Friedrichs extension; the spectral theorem for self-adjoint operators; spectral theory for Schrödinger operators.

**Prerequisites:** MA 646 [Min Grade: B]

**MA 748. Fourier Transforms. 3 Hours.**

Fourier transform and inverse transform to tempered distributions; applications to partial differential equations.

**Prerequisites:** MA 645 [Min Grade: B] and MA 655 [Min Grade: B]

**MA 749. Theory of Distribution. 3 Hours.**

The space of test functions. The space of distributions. Main properties of distributions. Completeness of the space of distributions. Support of a distribution. Sochozki formula. Derivatives of distributions and their properties. The structure of a distribution with a point support. Direct products and convolutions of distributions and their properties. Regularization of distributions. The space of test functions of rapid decay. The space of distributions of slow growth and their properties. Fourier transform of test functions of rapid decay and its properties. Parseval's identity. Fourier transform of distributions of slow growth. Fourier transform of direct products and convolutions of distributions of slow growth. Applications of distributions to partial differential equations. Fundamental solutions of partial differential equations.

**Prerequisites:** MA 645 [Min Grade: B]

**MA 750. Advanced Ordinary Differential Equations. 3 Hours.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 753. Nonlinear Analysis. 3 Hours.**

Selected topics including degree theory, bifurcation theory, and topological methods.

**MA 755. Advanced Partial Differential Equations. 3 Hours.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**Prerequisites:** MA 645 [Min Grade: B]

**MA 760. Dynamical Systems I. 3 Hours.**

Continuous dynamical systems; limit sets; centers of attraction; recurrence; stable and wandering points; flow boxes, and monotone sequences in planar dynamical systems; Poincare-Bendixson theorem.

**MA 761. Dynamical Systems II. 3 Hours.**

Discrete dynamical systems; hyperbolicity; symbolic dynamics; chaos; homoclinic orbits; bifurcations; attractors(theory and examples).

**MA 770. Continuum Theory. 3 Hours.**

Pathology of compact connected metric spaces; inverse limits; boundary bumping theorem; Hahn-Muzukiewicz theorem; composants; chainable and circle-like continua; irreducibility; separation; unicoherence; indecomposability.

**MA 772. Complex Analytic Dynamics. 3 Hours.**

Riemann surfaces; polynomial dynamics, rational functions and entire functions; fixed point theory; Mandelbrot set; Julia sets; prime ends; conformal mappings.

**MA 774. Algebraic Topology. 3 Hours.**

Covering spaces; introduction to homotopy theory; singular homology, cohomology.

**MA 776. Advanced Differential Geometry. 3 Hours.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 781. Differential Topology I. 3 Hours.**

A study of differentiable structures on manifolds, primarily from a global viewpoint: smooth mappings including diffeomorphisms, immersions and submersions; submanifolds and transversality.

**Prerequisites:** MA 645 [Min Grade: B] and MA 675 [Min Grade: B]

**MA 782. Differential Topology II. 3 Hours.**

A continuation of MA 781, with further applications such as Morse Theory.

**MA 790. Mathematics Seminar. 1-3 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 791. Mathematics Seminar. 1-3 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 792. Special Topics in Mathematics. 1-3 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 793. Special Topics in Mathematics. 1-3 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 794. Special Topics in Mathematics. 1-6 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 795. Special Topics in Mathematics. 1-6 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 796. Special Topics in Mathematics. 1-12 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 797. Special Topics in Mathematics. 1-12 Hour.**

This course covers special topics in mathematics and the applications of mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 798. Non-Dissertation Research and Preparation for Comp. 1-12 Hour.**

This course covers special topics in mathematics and the applications of the mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**MA 799. Dissertation Research. 1-12 Hour.**

This course covers special topics in mathematics and the applications of the mathematics. May be repeated for credit when topics vary. Prerequisites vary with topics.

**Prerequisites:** GAC Z